

# Package: DRquality (via r-universe)

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**Type** Package

**Title** Quality Measurements for Dimensionality Reduction

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**Maintainer** Michael Thrun <m.thrun@gmx.net>

**Description** Several quality measurements for investigating the performance of dimensionality reduction methods are provided here. In addition a new quality measurement called Gabriel classification error is made accessible.

**License** GPL-3

**Imports** DatabionicSwarm

**Suggests** plotly, geometry, deldir, FCPS, ProjectionBasedClustering, DataVisualizations, FastKNN, ggplot2, pcaPP, pracma, spdep, grid, igraph, ccccd, sf

**LazyData** TRUE

**Encoding** UTF-8

**Repository** <https://mthrun.r-universe.dev>

**RemoteUrl** <https://github.com/mthrun/drquality>

**RemoteRef** HEAD

**RemoteSha** f633c77789563234b9f2ad7c6c125c4049638d92

## Contents

ClassificationError . . . . .	2
Cmeasure . . . . .	3
GabrielClassificationError . . . . .	4
KendallsTau . . . . .	6
plotMeasureRAAR . . . . .	7
plotMeasureTundD . . . . .	7
RAAR . . . . .	8
SpearmanError . . . . .	9

Spearman's Rho . . . . .	9
Topological Correlation . . . . .	10
ZrechenMeasure4All . . . . .	11

<b>Index</b>	<b>13</b>
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ClassificationError	<i>Classification Error (rate)</i>
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### Description

Compares projected points to a given prior classification using knn classifier.

### Usage

```
ClassificationError(OutputDistances, Cls, k=5)
```

### Arguments

OutputDistances	[1:n,1:n]
Cls	[1:n]
k	number of k nearest neighbors, in Venna 2010 set to 5 (here default)

### Details

Projected points are evaluated by k-nearest neighbor classification accuracy (with  $k = 5$ ), that is, each sample in the visualization is classified by majority vote of its  $k$  nearest neighbors in the visualization, and the classification is compared to the ground truth label. [Venna 2010].

### Value

Error	Classification Error: 1-Accuracy[1]
Accuracy	Accuracy
KNNCls	[1:n] cls of knn classifier

### Note

Here, the Outputdistances of the Projected points are used.

### Author(s)

Michael Thrun

**References**

Venna, J., Peltonen, J., Nybo, K., Aidos, H., and Kaski, S. Information retrieval perspective to non-linear dimensionality reduction for data visualization. *The Journal of Machine Learning Research*, 11, 451-490. (2010)

Gracia, A., Gonzalez, S., Robles, V., and Menasalvas, E. A methodology to compare Dimensionality Reduction algorithms in terms of loss of quality. *Information Sciences*, 270, 1-27. (2014)

**Examples**

```
if(requireNamespace("FCPS")){
  data(Hepta,package="FCPS")
  projection=cmdscalet(dist(Hepta$Data), k=2)
  ClassificationError(as.matrix(dist(projection)),Hepta$Cls)
}
```

Cmeasure

*C-Measure subtypes***Description**

Calculate the C-Measure subtypes of minimal path length and minimal wiring

**Arguments**

Data	[1:n,1:d] numerical matrix of points in input space.
Projection	[1:n,1:2] numerical matrix of points in output space.
k	Number of nearest neighbors, both measures set it always to k=1.

**Value**

[[1:2] Numerical vector of MinimalPathlength and MinimalWiring values.

**Author(s)**

Michael Thrun

**Examples**

```
if(requireNamespace("FCPS")){
  data(Hepta,package="FCPS")
  projection=cmdscalet(dist(Hepta$Data), k=2)
  Cmeasure(Hepta$Data,projection)
}
```

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 GabrielClassificationError

*Gabriel Classification Error (GCE)*


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### Description

GCE searches for the k-nearest neighbors of the first gabriel neighbors weighted by the Euclidean Distances of the Inputspace [Thrun et al, 2023]. GCE evaluates these neighbors in the Output space. A low value indicates a better two-dimensional projection of the high-dimensional Input space.

### Usage

```
GabrielClassificationError(Data,ProjectedPoints,Cls,LC,
PlotIt=FALSE,Plotter = "native", Colors = NULL,LineColor= 'grey',
main = "Name of Projection", mainSize = 24,xlab = "X", ylab = "Y", xlim, ylim,
pch,lwd,Margin=list(t=50,r=0,l=0,b=0))
```

### Arguments

Data	[1:n,1:d] Numeric matrix with n cases and d variables
ProjectedPoints	[1:n,1:2] Numeric matrix with 2D points in cartesian coordinates
Cls	[1:n] Numeric vector with class labels
LC	Optional, Numeric vector of two values determining grid size of the underlying projection
PlotIt	Optional, Boolean: TRUE/FALSE => Plot/Do not plot (Default: FALSE)
Plotter	Optional, Character with plot technique (native or plotly)
Colors	Optional, Character vector of class colors for points
LineColor	Optional, Character of line color used for edges of graph
main	Optional, Character plot title
mainSize	Optional, Numeric size of plot title
xlab	Optional, Character name of x ax
ylab	Optional, Character name of y ax
xlim	Optional, Numeric vector with two values defining x ax range
ylim	Optional, Numeric vector with two values defining y ax range
pch	Optional, Numeric of point size (graphic parameter)
lwd	Optional, Numeric of linewidth (graphic parameter)
Margin	Optional, Margin of plotly plot

**Details**

Gabriel classification error (GCE) makes an unbiased evaluation of distance and densitybased structure which may be even non-linear separable. First, GCE utilizes the information provided by a prior classification to assess projected structures. Second, GCE applies the insights drawn from graph theory. Details are described in [Thrun et al, 2023]

**Value**

list of

GCE	GabrielClassificationError NOTE the rest is just for development purposes
GCEperPoint	[1:n] unnormalized GCE of each point: $GCE = \text{mean}(GCEperPoint)$
nn	the number of points in a relevant neighborhood: $0.5 * 85\text{percentile}(AnzNN)$
AnzNN	[1:n] the number of points with a gabriel graph neighborhood
NNdists	[1:n,1:nn] the distances within the relevant neighborhood, 0 for inner cluster distances
HD	[1:nn] HD = HarmonicDecay(nn) i.e weight function for the NNdists: $GCEperPoint = HD * NNdists$
IsInterDistance	Distances to the nn closest neighbors
GabrielDists	Distance matrix implied by high dimensional distances and the underlying gabriel (Gabriel) graph
ProjectionGraphError	Plotly object in case, plotly is chose

**Author(s)**

Michael Thrun, Quirin Stier, Julian Märte

**References**

[Thrun et al, 2023] Thrun, M.C, Märte, J., Stier, Q.: Analyzing Quality Measurements for Dimensionality Reduction, Machine Learning and Knowledge Extraction (MAKE), Vol 5., accepted, 2023.

**Examples**

```
if(requireNamespace("FCPS")){
  data(Hepta,package="FCPS")
  projection=cmdscales(dist(Hepta$Data), k=2)
  GabrielClassificationError(Hepta$Data,projection,Hepta$Cls)$GCE
}
```

```
if(requireNamespace("FCPS")){
  data(Hepta,package="FCPS")
  projection=cmdscales(dist(Hepta$Data), k=2)
  GabrielClassificationError(Hepta$Data,projection,Hepta$Cls)$GCE
}
```

```
}
```

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KendallsTau	<i>Statistical correlation by Kendall</i>
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### Description

Calculates the statistical correlation by Kendall. Basically a wrapper to `pcaPP::cor.fk`.

### Usage

```
KendallsTau(InputDists, OutputDists)
```

### Arguments

`InputDists` Matrix containing the distances of the first dataset.  
`OutputDists` Matrix containing the distances of the second dataset.

### Value

Equivalent to `cor.fk`

### Author(s)

Michael Thrun

### Examples

```
if(requireNamespace("FCPS")){  
  data(Hepta,package="FCPS")  
  InputDist=dist(Hepta$Data)  
  projection=cmdscale(InputDist, k=2)  
  KendallsTau(as.matrix(InputDist),as.matrix(dist(projection)))  
}
```

---

plotMeasureRAAR      *Computes rank-based smoothed precision and recall*

---

### Description

Compares the projection in pData with the original data in Data and calculates trustworthiness and continuity of the projection for neighborhood sizes ranging from 1 to the size of the neighborhood.

### Usage

```
plotMeasureRAAR(Raar, label = 'ProjectionMethod',
gPlotList = list(RAARplot = ggplot2::ggplot()), LineType="solid", Shape = 16,
PointsPerE = 10, fancy = FALSE)
```

### Arguments

Raar	Output of RAAR() applied for a projection method.
label	Title of plot.
gPlotList	Settings for ggplot.
LineType	Character - graphic parameter: Line type of ggplot.
Shape	Integer: type of point
PointsPerE	Numeric graphic parameter: Distance between markers on plot line
fancy	Boolean graphic parameter: Some automatic settings for a more appealing plot.

### Value

ggplot object

### Author(s)

Michael Thrun

---

plotMeasureTundD      *Computes rank-based smoothed precision and recall*

---

### Description

Compares the projection in pData with the original data in Data and calculates trustworthiness and continuity of the projection for neighborhood sizes ranging from 1 to the size of the neighborhood.

### Usage

```
plotMeasureTundD(TDmatrix, label = 'ProjectionMethod',
gPlotList = list(TW = ggplot2::ggplot(), DC = ggplot2::ggplot()), LineType = "solid",
Shape = 16, PointsPerE = 16)
```

**Arguments**

TDmatrix	Output of MeasureTundD() applied for a projection method.
label	Title of plot.
gPlotList	Settings for ggplot.
LineType	Character - graphic parameter: Line type of ggplot.
Shape	Integer: type of point
PointsPerE	Numeric graphic parameter: Distance between markers on plot line

**Value**

ggplot object

**Author(s)**

Michael Thrun

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RAAR

*Rescaled average agreement rate*

---

**Description**

Rescaled average agreement rate deduced by the co-ranking matrix from LCMC.

**Usage**

```
RAAR(Data, ProjectedPoints, kmax = nrow(Data) - 2, PlotIt = T)
```

**Arguments**

Data	Matrix containing n cases in rows, d variables in columns or a distance matrix which in this case has to be symmetric
ProjectedPoints	n by OutputDimension matrix containing coordinates of the Projection
kmax	maximum of intervall 1:kmax of k nearest neighbors
PlotIt	Optional: Should the output be plottet. Default: TRUE

**Value**

A list containing:

Raar	Rescaled average agreement rate
Aar	Average agreement rate

**Author(s)**

Michael Thrun



**References**

Lee, J. A., Peluffo-Ordonez, D. H., & Verleysen, M. Multiscale stochastic neighbor embedding: Towards parameter-free dimensionality reduction. Paper presented at the Proceedings of 22st European Symposium on Artificial Neural Networks, Computational Intelligence And Machine Learning (ESANN) (2014).

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SpearmanError	<i>Calculates the error of a projection with spearman's rank correlation coefficient</i>
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**Description**

Calculates the error of a projection with spearman's rank correlation coefficient.

**Arguments**

VectorOfInputDists(1:n2)  
dissimilarities in Input Space between the n data points in vector form as produced by squareform(Dists(1:n,1:n))

VectorOfOutputDists(1:n2)  
dissimilarities in Input Space between the n data points in vector form as produced by squareform(Dists(1:n,1:n))

**Value**

rho rank correlation coefficient

**Author(s)**

Florian Lerch

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Spearman's Rho	<i>Calculates the error of a projection with spearman's rank correlation coefficient</i>
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**Description**

Calculates the error of a projection with spearman's rank correlation coefficient

**Usage**

Spearman's Rho(InputDists, OutputDists)

**Arguments**

InputDists      [1:d,1:d] numeric matrix with input distances  
 OutputDists    [1:d,1:d] numeric matrix with output distances

**Value**

rho

**Author(s)**

Julian Märte

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TopologicalCorrelation

*Topological Correlation*

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**Description**

Calculates the Topological Correlation

**Usage**

TopologicalCorrelation(Data,ProjectedPoints,type='norm',method,Kn=0)

**Arguments**

Data            a matrix of the given n-dim. points: the rows represent the points and the columns represent the coordinates in the n-dim. space.

ProjectedPoints  
 matrix of Projected Points, if missing, method should be set!

method        Determines whether the selected projections method for a given set of n-Dim. points is a good choice. Therefor, a result of 1 means the selected projections method is good, and a result value of 0 means that the Visualization of the given Data in the two dim. space doesnt fit for the problem.

type          How the paths in the adjacencematrix should be weighted, norm represents path lengths of 1 and euclidean represents the distance in the euclidean metric.

Kn            k nearest neighbours in the graph. only needed in method is isomap and LocallyLinearEmbedding

**Value**

TC value

**Author(s)**

Hermann Tafo, Laukert Schlichting 07/2015

**Examples**

```

if(requireNamespace("FCPS")){
  data(Hepta,package="FCPS")
  projection=cmdscale(dist(Hepta$Data), k=2)
  TopologicalCorrelation(Hepta$Data,projection)
}

```

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ZrehenMeasure4All      *A generalized version of the zrehen-measure which defines the neighbourhood by gabrielgraph and is therefore not restricted to grid-based projections.*

---

**Description**

A generalized version of the zrehen-measure which defines the neighbourhood by gabrielgraph and is therefore not restricted to grid-based projections.

**Arguments**

Data	[1:n,1:d] points in input room with d attributes
Projection	[1:n,1:2] projected points in output room, with index,x,y or index,line,column
width	only necessary if toroid
height	only necessary if toroid
isToroid	are the points toroid?
isGrid	is the grid a toroid?
plotGabriel	plot the generated GabrielGraph

**Value**

List with

V\$zrehen	the raw zrehen measure
V\$normedzrehen	the zrehen measure normed by the number of neighbours
v\$neighbourcounter	the number of possible neighbours by which the zrehen measure is normed

**Author(s)**

Florian Lerch 07/2015

**Examples**

```
if(requireNamespace("FCPS")){  
  data(Hepta,package="FCPS")  
  projection=cmdscale(dist(Hepta$Data), k=2)  
  ZrehenMeasure4All(Hepta$Data,projection)$zrehen  
}
```

# Index

- \* **Classification Error**
    - ClassificationError, [2](#)
    - GabrielClassificationError, [4](#)
  - \* **ClassificationErrorRate**
    - ClassificationError, [2](#)
  - \* **ClassificationError**
    - ClassificationError, [2](#)
  - \* **Evaluation of projection methods**
    - GabrielClassificationError, [4](#)
  - \* **GCE**
    - GabrielClassificationError, [4](#)
  - \* **Gabriel Classification Error**
    - GabrielClassificationError, [4](#)
  - \* **QM**
    - GabrielClassificationError, [4](#)
  - \* **Quality measurement**
    - GabrielClassificationError, [4](#)
  - \* **Quality measure**
    - GabrielClassificationError, [4](#)
- ClassificationError, [2](#)  
Cmeasure, [3](#)  
cor.fk, [6](#)
- GabrielClassificationError, [4](#)
- KendallsTau, [6](#)
- plotMeasureRAAR, [7](#)  
plotMeasureTundD, [7](#)
- RAAR, [8](#)
- SpearmanError, [9](#)  
SpearmanRho, [9](#)
- TopologicalCorrelation, [10](#)
- ZrehenMeasure4All, [11](#)